



A/B Testing under Network Interference

A unit's potential outcome is not only decided by its own assigned treatment, but also **treatments assigned to its neighbors on network.**

With classical neighborhood interference assumption (in violation of SUTVA), we have:

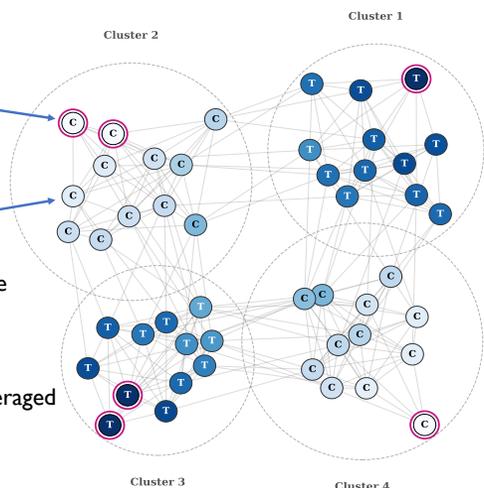
$$Y_i = Y_i(z_i; \{z_j : A_{ij} = 1\})$$

Leveraging Interior Units: A Tale of Semi-Supervision in Network Experiments

High-quality labeled sample: **interior nodes**, whose exposure levels always equal 0/1 and can be viewed as ground-truth in estimating Global ATE.

Low-quality pseudo-labeled sample: **boundary nodes**, the majority of whole population.

Though being biased samples due to network interference, they can be leveraged to reduce the **selection bias of cluster interior**, through PPI-type adjustment.



Problem of Existing Estimators

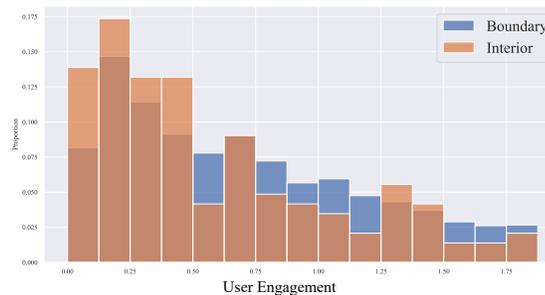
- Overdependency on interior nodes
- High-variance for statistical estimators, and high-bias for regression-based estimator

Mean-in-Interior (MII) Estimator: Difference-in-Means for Interior Nodes

$$\hat{\tau}_{MII} = \frac{\sum_{i \in \text{Int}} z_i Y_i}{\sum_{j \in \text{Int}} z_j} - \frac{\sum_{i \in \text{Int}} (1 - z_i) Y_i}{\sum_{j \in \text{Int}} (1 - z_j)}$$

- **Reduces variance** with moderate weights (in comparison to inverse propensity weight, exponentially scale w.r.t. a unit's degree).
- Still incurs **selection bias** due to discrepancy between interior and boundary units.

Empirical evidence of discrepancy



Augmented MII Estimator: Leveraging Boundary Nodes for Debiasing Adjustment

$$\hat{\tau}_{AMII} = \hat{\tau}_{MII} + \left(\frac{1}{n} \sum_{j \in [n]} f(\mathbf{1}, X, A)_j - \frac{1}{s_1} \sum_{i \in \text{Int}} z_i f(\mathbf{1}, X, A)_i \right) - \left(\frac{1}{n} \sum_{j \in [n]} f(\mathbf{0}, X, A)_j - \frac{1}{s_0} \sum_{i \in \text{Int}} (1 - z_i) f(\mathbf{0}, X, A)_i \right)$$

- Train a counterfactual predictor f for removing the selection bias of MII estimator.
- Intuition: regression component for capturing covariates; MII for capturing network exposure at two terminals (global 0/1). **Debiasing using predictions.**

Experiments performance: Bias, Std, MSE

